

Fuzzy Logic Controller for Enhancement of Transient Stability in Multi Machine AC-DC Power Systems

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Abstract— This paper discusses the impact of HVDC on Power System Stability and proposes a new type of control mechanism based on Fuzzy set theory to augment dynamic performance of a multi-machine power system. To have good damping characteristics over a wide range of operating conditions, speed deviation ($\Delta\omega = \text{error}_1$) and acceleration ($\Delta\dot{\omega} = \text{error}_3$), of the machines are chosen as the input signals to the fuzzy controller. These input signals are first characterized by a set of linguistic variables using fuzzy set notations. The fuzzy relation matrix allows a set of fuzzy logic operations that are performed on controller inputs to obtain the desired output. The effectiveness of the proposed controller is demonstrated by a multi-machine system example. The superior performance of this fuzzy controller in comparison to the conventional fixed gain controller proves the efficiency of this new fuzzy PID controller.

Keywords – *HVDCT, Power System Stability, Multi-Machine Stability, Fuzzy Logic Controller*

I. INTRODUCTION

The choice between transmission alternatives is made on the basis of cost and controllability. The original justification for HVDC systems was its lower cost for long electrical distances, which, in the case of submarine (or underground) cable schemes, applies to relatively short geometrical distances. At present, the controllability factor justifies the DC alternative regardless of cost as evidenced by the growing number of back-to-back links in existence. HVDC systems have the ability to rapidly control the transmitted power. Therefore, they have a significant impact on the stability of the associated AC Power Systems. More importantly, proper design of the HVDC controls is essential to ensure satisfactory performance of overall AC/DC system [1]. In recent years, the HVDC system models used are simpler models; such models are adequate for general purpose stability studies of systems in which the DC link is connected to stronger parts of the AC system. But the preference is to have a flexible modeling capability with a required range of detail [2].

Supplementary controls are often required to exploit the controllability of DC links for enhancing the AC system dynamic performance. There are a variety of such higher level controls used in practice. Their performance objectives vary depending on the characteristics of the associated AC systems. The controls used tend to be unique to each system. To date, no attempt has been made to develop generalized control schemes applicable to all systems.

The supplementary controls use signals derived from the AC systems to modulate the DC quantities. The modulating signals may be derived from tie-line power flow, relative angular deviations of the machines, relative speed deviations

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of the machines and average difference in accelerations of the machines. The particular choice depends on the system characteristics and the desired results. In this paper, apart from conventional controllers, a fuzzy logic based controller is developed to modulate the power order of the DC control, which in turn modulates the DC power.

II. AC/DC STABILITY ANALYSIS

In transient stability studies, it is prerequisite to do AC/DC load flow calculations in order to obtain system conditions prior to the disturbance. The eliminated variable method proposed in [3] is used here, which treats the real and reactive powers consumed by the converters as voltage dependent loads. The DC equations are solved analytically or numerically and the DC variables are eliminated from the power flow equations. The method is unified, since the effect of the DC-link is included in the Jacobian. It is, however, not an extended variable method, since no DC variables are added to the solution vector.

A. DC System Model

The equations describing the steady state behavior of a mono polar DC link can be summarized as follows[1-3]:

$$V_{dr} = \frac{3\sqrt{2}}{\pi} a_r V_{tr} \cos \alpha_r - \frac{3}{\pi} X_c I_d \quad (1)$$

$$V_{di} = \frac{3\sqrt{2}}{\pi} a_i V_{ti} \cos \gamma_i - \frac{3}{\pi} X_c I_d \quad (2)$$

$$V_{dr} = V_{di} + r_d I_d \quad (3)$$

$$P_{dr} = V_{dr} I_d \quad (4)$$

$$P_{di} = V_{di} I_d \quad (5)$$

$$S_{dr} = k \frac{3\sqrt{2}}{\pi} a_r V_{tr} I_d \quad (6)$$

$$S_{di} = k \frac{3\sqrt{2}}{\pi} a_i V_{ti} I_d \quad (7)$$

$$Q_{dr} = \sqrt{S_{dr}^2 - P_{dr}^2} \quad (8)$$

$$Q_{di} = \sqrt{S_{di}^2 - P_{di}^2} \quad (9)$$

Where , k is assumed constant and is given by the relation $k = (\Pi/3*\sqrt{2})*(I_{ac}/I_d)$, $k \approx 0.995$.

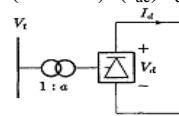


Fig-1:Model of DC converter

B .The Eliminated Variable Method

The real and reactive powers consumed by the converters are written as functions of V_{tr} and V_{ti} . The expressions for their partial derivatives with respect to V_{tr} and V_{ti} are computed and used in modification of Jacobian elements of the Newton Raphson power flow as shown below:

$$\begin{bmatrix} \Delta P \\ \Delta Q \end{bmatrix} = \begin{bmatrix} H & N \\ J & L \end{bmatrix} \begin{bmatrix} \Delta \delta \\ \Delta V/V \end{bmatrix} \quad (10)$$

$$N'(tr,tr) = V_{tr} \frac{\partial P_{tr}^{ac}}{\partial V_{tr}} + V_{tr} \frac{\partial P_{dr}(V_{tr}, V_{ti})}{\partial V_{tr}} \quad (11)$$

$$N'(tr,ti) = V_{tr} \frac{\partial P_{tr}^{ac}}{\partial V_{ti}} + V_{tr} \frac{\partial P_{dr}(V_{tr}, V_{ti})}{\partial V_{ti}} \quad (12)$$

$$N'(ti,tr) = V_{ti} \frac{\partial P_{ti}^{ac}}{\partial V_{tr}} - V_{tr} \frac{\partial P_{di}(V_{tr}, V_{ti})}{\partial V_{tr}} \quad (13)$$

$$N'(ti,ti) = V_{ti} \frac{\partial P_{ti}^{ac}}{\partial V_{ti}} - V_{ti} \frac{\partial P_{di}(V_{tr}, V_{ti})}{\partial V_{ti}} \quad (14)$$

L' is modified analogously. Thus, in the eliminated variable method, four mismatch equations and upto eight elements of the Jacobian have to be modified, but no new variables are added to the solution vector, when a DC-link is included in the power flow.

C. Representation of HVDC Systems

Each DC system tends to have unique characteristics tailored to meet the specific needs of its application. Therefore, standard models of fixed structures have not been developed for representation of DC systems in stability studies.

The current controller employed here (fig.2) is a proportional integral controller and the auxiliary controller is taken to be a constant gain controller.

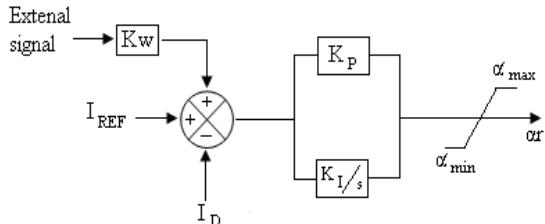


Fig-2: Current controller and auxiliary controller

HVDC line is represented using transfer function model [4] as shown in the figure 3.

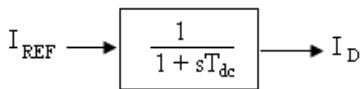


Fig-3: Transfer function model

In this case, the time constant of the DC link T_{dc} ($= L_{dc}/R_{dc}$) represents the delay in establishing the DC current after a step change in the order is given.

D. Generator Representation

The synchronous machine is represented by a voltage source, behind a transient reactance, that is constant in magnitude but changes in angular position.

$$\frac{d\delta}{dt} = \omega - 2\pi f \quad (15)$$

$$\frac{d^2\delta}{dt^2} = \frac{d\omega}{dt} = \frac{\pi f}{H} (P_m - P_e)$$

E. Representation of Loads

The static admittance Y_{po} used to represent the load at bus-p, can be obtained from

$$Y_{po} = \frac{I_{po}}{E_p} \quad \text{where, } I_{po} = \frac{P_{lp} - jQ_{lp}}{E_p^*} \quad (16)$$

F. Steps of the AC-DC Transient Stability Study

Generally, the DC scheme interconnects two or more, otherwise independent, AC systems and the stability assessment is carried out for each of them separately, taking into account the power constraints at the converter terminal. If the DC link is part of a single (synchronous) AC system, the converter constraints will apply to each of the nodes containing a converter terminal. The basic structure of transient stability program is given below [5]:

- 1) The initial bus voltages are obtained from the AC/DC load flow solution prior to the disturbance.
- 2) After the AC/DC load flow solution is obtained, the machine currents and voltages behind transient reactance are calculated.
- 3) The initial speed is equated to $2\pi f$ and the initial mechanical power is equated to the real power output of each machine prior to the disturbance.
- 4) The network data is modified for the new representation. Extra nodes are added to represent the generator internal voltages. Admittance matrix is modified to incorporate the load representation.
- 5) Set time, $t=0$;
- 6) If there is any switching operation or change in fault condition, modify network data accordingly and run the AC/DC load flow.
- 7) Using Runge-Kutta method, solve the machine differential equations to find the changes in the internal voltage angle and machine speeds.
- 8) Internal voltage angles and machine speeds are updated and are stored for plotting.
- 9) AC/DC load flow is run to get the new output powers of the machine.
- 10) Advance time, $t=t+\Delta t$.
- 11) Check for time limit, if $t \leq t_{max}$ repeat the process from step 6, else plot the graphs of internal voltage angle variations and stop the process.

Basing on the plots, that we get from the above procedure it can be decided whether the system is stable or unstable. In

case of multi machine system stability analysis the plot of relative angles is done to evaluate the stability.

III. CONVENTIONAL CONTROLLER

The WSCC 3-Machine, 9-Bus system [6] is considered for the stability analysis and is given in figure-4.

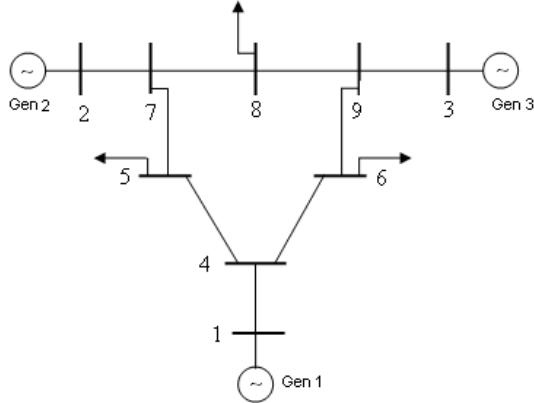


Fig-4: WSCC three-machine, nine-bus system

A HVDC line is assumed to be present between buses 4–5. A three phase to ground fault is assumed to occur on the line 4 – 6, near to bus-6, at initial time zero. It is cleared after 4 cycles, by removing the line and to reflect this removal the admittance matrix is modified. Initially, HVDC line is assumed to maintain same control as it had in the normal condition. The power flowing through the HVDC link is maintained constant and equal to pre-fault value. Then the plot of relative angles is as shown in figure-5.

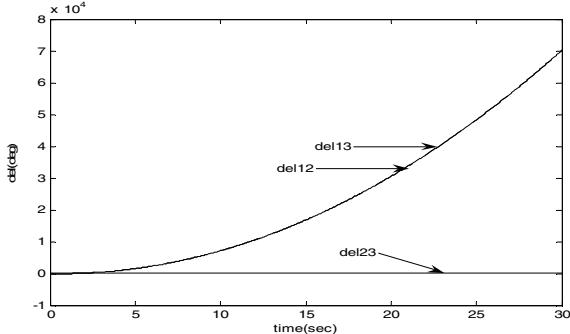


Fig-5: Plot of relative angles without any control

From the figure it is clear that the system is unstable as the relative angles are increasing. It can be examined that the generator-1 is going out of step with respect to the generators 2 and 3. To stabilize the system it is necessary to make the accelerations of all the generators equal. So an error signal representing average difference in accelerations of the generators is considered. In case of multi-machine systems the relative angles are to be maintained within limits to maintain the stability of the system. So, error signals derived from the average difference in the relative angles and average difference in the relative speeds of the generators are considered. These error signals are as shown below:

$$error_1 = \left[\left[\frac{(\omega(2) - \omega(1)) + (\omega(3) - \omega(1))}{2} \right] - [\omega(2) - \omega(3)] \right] \quad (17)$$

$$error_2 = \left[\left[\frac{(del(2) - del(1)) + (del(3) - del(1))}{2} \right] - [del(2) - del(3)] \right] \quad (18)$$

$$error_3 = \left[\frac{P_{mis}(3) + P_{mis}(2)}{H(3) + H(2)} - \left[\frac{P_{mis}(1)}{H(1)} \right] \right] \quad (19)$$

Different combinations of the above three signals are considered, in order to improve the stability. Gains of the signals are varied in order to get better transient and dynamic performance. When $error_3$ signal is considered for improving the stability of the system as suggested in [2], the plot of relative angles is shown in figure-6. This reveals that the considered signal is inadequate to improve the stability of the system.

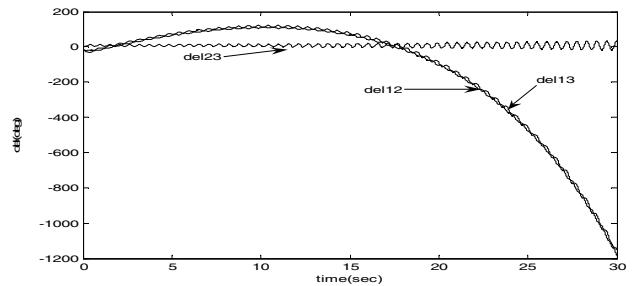


Fig-6: Plot of relative angles with $error_3$ as control signal

Considering the different combinations of the signals in varied proportions, as the control input, the plot of relative angles are as shown in figures: 6(a),6(b)&6(c).

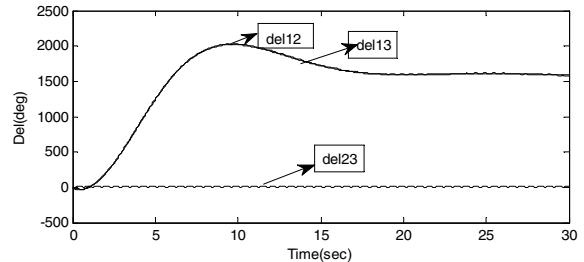


Fig-6.(a): Plot of relative angles with control signal $K_p * error_1 + K_i * error_2$

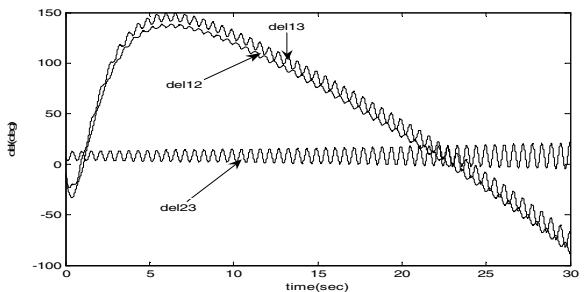


Fig-6-(b): Plot of relative angles with control signal $K_p * error_1 + K_d * error_3$

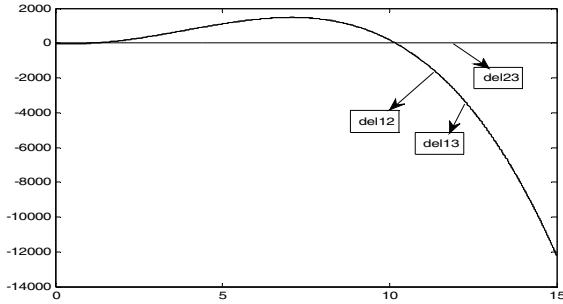


Fig-6(c): Plot of relative angles with ΔP_{ac} (tie-line power change) as control signal

In the above cases it can be seen that either the system is unstable or there is no considerable improvement in the stability of the system. When all the three signals are considered, the plot of the relative angles is as shown in figure-7. It can be seen that the stability of the system is improved and by the end of the study time the action of AGC will come into picture which will further improve the system stability.

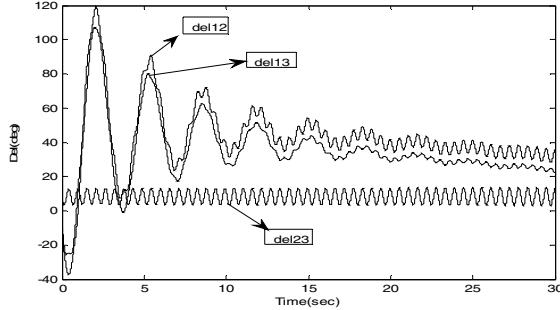


Fig-7: Plot of relative angles with control signal
 $K_p * \text{error}_1 + K_i * \text{error}_2 + K_d * \text{error}_3$

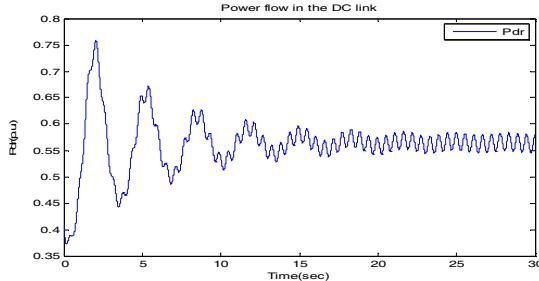


Fig-8: Plot of DC power (with conventional PID controller)

Control signal is given by the following expression:

$$\text{error} = K_p * \text{error}_1 + K_i * \text{error}_2 + K_d * \text{error}_3 \quad (20)$$

So, for this formulation of the system and for this disturbance scenario it is essential to use all the three signals, to have a considerable improvement in the stability of the system. Here, the signal error_2 is the equivalent to the integral of the signal error_1 , and the signal error_3 is equivalent to the differential of the signal error_1 . Hence, the controller proposed above is equivalent to a PID controller. Then the control signal can be equivalently represented as in equation (21).

$$\text{error} = K_p * e(t) + K_i * Ie(t) + K_d * De(t) \quad (21)$$

IV. FUZZY LOGIC CONTROLLER

Here a fuzzy logic controller is used with the error_1 and error_3 as its inputs and the resultant error of the PID control scheme has been adopted as input for the purpose of enhancing the stability of multi-machine power systems, utilizing HVDC power modulation. In this scheme, the error signals error_1 and error_3 control signals as specified in the previous section, are fuzzified at very sampling interval, in accordance to a set of linguistic control rules and in conjunction with fuzzy logic and output fuzzy value is defuzzified using min-max method. This feature is desirable because as the operating conditions of a system begin to change, deterioration in performance will result if a fixed gain controller is applied. Consequently, the proposed control scheme has the advantages of a conventional PID controller and that of a fuzzy logic controller.

A. Fuzzy Relation

Let A and B be two fuzzy sets with membership functions $\mu_A(x)$ and $\mu_B(x)$, respectively. A fuzzy relation R from A to B can be visualized as a fuzzy graph and can be characterized by the membership function $\mu_R(x,y)$ which satisfies the composition rule as follows:

$$\mu_B(y) = \max_x (\min(\mu_R(x,y) \mu_A(x))) \quad (22)$$

In many cases it is convenient to express the membership function of a fuzzy subset of the real line in terms of a standard function whose parameters may be adjusted to fit a specified membership function in a suitable fashion.

B. Design of the Fuzzy Controller for Power System Stability

To determine the controller output from the measured system variables error_1 and error_3 , a fuzzy relation matrix R, which gives the relationship between the fuzzy set characterizing inputs and the fuzzy set characterizer output, is computed as follows.

Step 1: Use membership functions to represent stabilizer inputs error_3 and error_1 in fuzzy set notation.

Step 2: Use the composition rule in eqn(22) to determine the membership function of the resultant error output.

Step 3: Determine a proper resultant error output from the membership function of the output signal.

Details of the above procedures are addressed in the following discussions.

C. Establishment of the Fuzzy Relation Matrix

A fuzzy relation matrix must be set up and stored in computer memory. A set of decision rules relating inputs to the output are first compiled. These decision rules are expressed using linguistic variables such as large positive (LP), medium positive (MP), small positive (SP), very small (VS), small negative (SN), medium negative (MN), and large negative (LN).

For example, a typical rule reads as follows:

Rule-1: If error_1 is LP and error_3 is LN, then $\text{error}_{\text{res}}$ should be VS. (23)

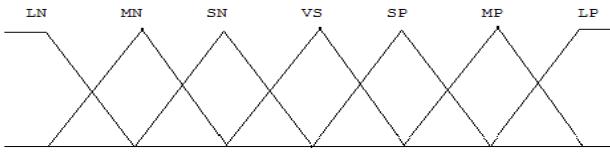


Figure-9: Membership function for 7 variables

Through the combination of the two input signals error_3 and error_1 , there will be 49 decision rules in all. The most convenient way to present these decision rules is to use a decision table as shown in Table-1. It is observed from Table-1 that each entry represents a particular rule.

Table-1: Decision table for seven membership variables

error_1	error_3						
	LN	MN	SN	VS	SP	MP	LP
LP	VS	SP	MP	LP	LP	LP	LP
MP	SN	VS	SP	MP	MP	LP	LP
SP	MN	SN	VS	SP	SP	MP	LP
VS	MN	MN	SN	VS	SP	MP	MP
SN	LN	MN	SN	SN	VS	SP	MP
MN	LN	LN	MN	MN	SN	VS	SP
LN	LN	LN	LN	LN	MN	SN	VS

Using these normalized quantities, controller inputs can be described by membership functions for the linguistic variables, as shown in Table-2. Note that only the membership functions for nine different values of error_3 and

error_1 are given in Table-2. For a value of error_3 or error_1 which is not listed in Table-2, linear interpolation must be employed to determine the membership function.

Table-2: Membership functions for inputs

Normalized error_1 and error_3	Membership functions						
	LN	MN	SN	VS	SP	MP	LP
-1.0	1	0.7	0.5	0.3	0	0	0
-0.2	1	0.9	0.7	0.5	0.2	0	0
-0.1	0.8	1	0.9	0.7	0.4	0.2	0
-0.05	0.6	0.8	1	0.9	0.6	0.4	0.2
0	0.4	0.6	0.8	1	0.8	0.6	0.4
0.05	0.2	0.4	0.6	0.9	1	0.8	0.6
0.1	0	0.2	0.4	0.7	0.9	1	0.8
0.2	0	0	0.2	0.5	0.7	0.9	1
1.0	0	0	0	0.3	0.5	0.7	1

Let us demonstrate the use of Table-2 by an example. At a particular sampling instant, let the sampled controller inputs be, say $\text{error}_1 = 0.2$ and $\text{error}_3 = -0.1$. From Table-2, the two controller inputs can be described by the following fuzzy sets:

$$\text{error}_1: \{(LN,0),(MN,0),(SN,0.2),(VS,0.5),(SP,0.7),(MP,0.9), (LP,1)\} \quad (24)$$

$$\text{error}_3: \{(LN,0.8),(MN,1),(SN,0.9),(VS,0.7),(SP,0.4),(MP,0.2), (LP,0)\} \quad (25)$$

D. Determination of the Resultant Error Output

Once the membership values for controller output have been computed, a suitable algorithm must be employed to determine the resultant error output signal. The algorithm adopted in this work is the 'maximum algorithm' in which the signal with largest membership value is chosen as the resultant error output signal. The resultant error output expressed in linguistic terms must be converted back to numerical values before it can be fed into the controller. The conversion table as shown in the Table-3 has been compiled based on the controller signals obtained in our previous work on the controller design. A different set of numerical values can be selected and different dynamic responses will be

obtained. The difference will however be insignificant since the error signal must be within the narrow range from -7.5 to 7. The table is stored in computer memory as a look-up table. It is observed from Table-3 that the numerical value of the stabilizing signal for our example is 1.8.

Table-3: Conversion table from 7 linguistic variables to numerical values

error _{res}	LN	MN	SN	VS	SP	MP	LP
-7.5	-5	-2.25	0.5	1.8	4.5	7	

Considering the above control strategy, the plots of relative rotor angles and DC power flow are as shown in figures: 9-10.

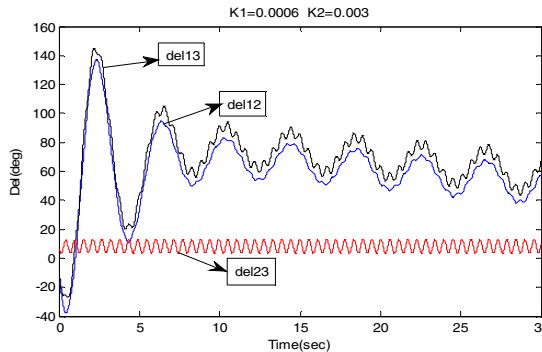


Figure-10: Plot of relative angles with proposed Fuzzy Logic controller (7 membership variables)

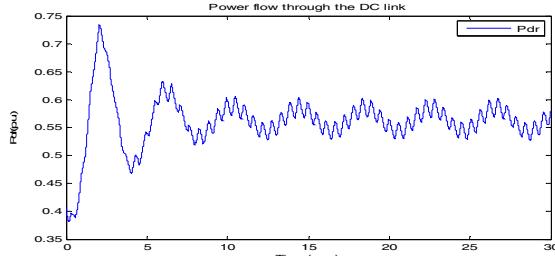


Fig-11: Plot of DC power (with Fuzzy controller-7 membership function)

V CONCLUSIONS

Considering the HVDC current controller and line dynamics, it is observed that the transient stability of the multi-machine system is improved only if the combination of all the three signals derived from relative speed, phase angle and average acceleration is used.

The paper presents a new approach to the design of a supplementary stabilizing controller for an HVDC transmission link using fuzzy logic. Results from this work reveal that, under disturbance conditions, better dynamic performance can be achieved using the proposed fuzzy controller than a conventional supplementary controller. Further improved performance can be obtained by suitably tuning the fuzzy controller. The proposed controller is very

simple for practical implementation since the decentralized output feedback control law developed in this paper requires only local measurements within each generating unit.

Research is being carried out to design a Hybrid Neuro-Fuzzy supplementary controller for two-terminal HVDC-AC systems for improvement of multi machine transient stability.

VI APPENDIX

DC Line Data: $r_d = 0.017\text{pu}$, $X_c = 0.6\text{pu}$, $L_d = 0.05\text{pu}$
 $\alpha_{\min} = 5^\circ$, $\alpha_{\max} = 80^\circ$, $\text{tap}_{r,\min} = 0.96$, $\text{tap}_{r,\max} = 1.06$
 $\text{tap}_{l,\min} = 0.99$, $\text{tap}_{l,\max} = 1.09$

Initial Conditions: $\alpha = 0.2094^\circ$, $I_d = 0.3691\text{pu}$, $P_{di} = 0.406\text{pu}$,
 $V_{di} = 1.1\text{pu}$, $V_{di} = 1.1\text{pu}$, $\gamma = 0.3142^\circ$
 $P_{M[1]} = 0.756646\text{pu}$, $P_{M[2]} = 1.63\text{pu}$, $P_{M[3]} = 1.63\text{pu}$
 $\delta_{M[1]} = 2.388448^\circ$, $\delta_{M[2]} = 18.603189^\circ$, $\delta_{M[3]} = 12.314856^\circ$

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